

## BIOGRAPHICAL SKETCH

Daniel Graham graduated from Middlebury College in 2001 with a major in physics and a minor in art history. He began graduate school in the physics department at Cornell University in the fall of the same year. For two years, he was a National Science Foundation IGERT fellow in the program in nonlinear dynamics. The IGERT program pursues questions involving chaotic, complex and nonlinear systems while taking an interdisciplinary approach. It was through the IGERT program that he learned about the work of Prof. David Field in the psychology department at Cornell, whose lab Mr. Graham officially joins in fall, 2004. Mr. Graham was also selected for the first group of NSF LOCNET fellows (2002) for which he worked in the biophysics lab of Prof. Michel Peyrard at the École Normale Supérieure in Lyon, France. In May, 2004, Mr. Graham organized a conference of science journalists and writers in order to explore the challenges and joys of communicating science to the general public. Many nationally-recognized writers spoke at the conference. Mr. Graham also plays club-level ultimate frisbee with LoG, a team based in Burlington, VT.

## ACKNOWLEDGMENTS

I wish to thank Prof. David Field for his patience and help with this thesis and Damon Chandler for his great assistance with coding. I also wish to thank my physics special committee: Prof. Sol Gruner, chair; Prof. Chris Henley; and Prof. Jim Alexander as well as Prof. Steve Strogatz of the IGERT program in nonlinear dynamics, which funded me for my first two years at Cornell.

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